

Kołowrocki Krzysztof

Soszyńska-Budny Joanna

Maritime University, Gdynia, Poland

Modelling critical infrastructure operation process including operating environment threats

Keywords

critical infrastructure, operation process, operating environment threats

Abstract

In the article the traditional semi-Markov approach to a complex technical system operation process modeling is developed to modelling a critical infrastructure operation process including operating environment threats. The method of defining the parameters of this operation process is presented and a new procedure of their determining in the case when the critical infrastructure operating threats are not explicit separated in this process is proposed.

1. Introduction

The operation process of a critical infrastructure is very complex and often it is difficult to analyze these critical infrastructure safety with respect to changing in time its operation process states and operating environment conditions that are essential in this analysis. The complexity of the critical infrastructure operation process and its influence on changing in time the critical infrastructure structure and its components' safety parameters are essential in critical infrastructure safety analysis and protection. Usually, the critical infrastructure environment have either an explicit or an implicit strong influence on the critical infrastructure operation process. As a rule, some of the environmental events together with the infrastructure operation conditions define a set of different operation states of the critical infrastructure in which the critical infrastructure change its safety structure and its components safety parameters. In this report, we propose a convenient tool for analyzing this problem applying the semi-Markov model [13]-[15], [17], [23]-[24] of the critical infrastructure operation process, both without including critical infrastructure environment threats and with including them into this model.

2. Modelling critical infrastructure operation process

We assume that the critical infrastructure during its operation process is taking $v, v \in N$, different operation states z_1, z_2, \dots, z_v . Further, we define the critical infrastructure operation process $Z(t)$, $t \in \langle 0, \infty \rangle$, with discrete operation states from the set

$\{z_1, z_2, \dots, z_v\}$. Moreover, we assume that the critical infrastructure operation process $Z(t)$ is a semi-Markov process [15], [22], [23]-[25] with the conditional sojourn times θ_{bl} at the operation states

z_b when its next operation state is z_l , $b, l = 1, 2, \dots, v$, $b \neq l$. Under these assumptions, the critical infrastructure operation process may be described by:

- the vector $[p_b(0)]_{1 \times v}$ of the initial probabilities $p_b(0) = P(Z(0) = z_b)$, $b = 1, 2, \dots, v$, of the critical infrastructure operation process $Z(t)$ staying at particular operation states at the moment $t = 0$;

- the matrix $[p_{bl}]_{v \times v}$ of probabilities p_{bl} , $b, l = 1, 2, \dots, v$, of the critical infrastructure operation process $Z(t)$ transitions between the operation states z_b and z_l ;

- the matrix $[H_{bl}(t)]_{v \times v}$ of conditional distribution functions $H_{bl}(t) = P(\theta_{bl} < t)$, $b, l = 1, 2, \dots, v$, of the

critical infrastructure operation process $Z(t)$ conditional sojourn times θ_{bl} at the operation states.

3. Modelling critical infrastructure operation process including operating environment threats

The companies (stakeholders, operators) using different critical infrastructures often have very different organizational environments. The critical infrastructures organizational environments are composed of forces or institutions surrounding an organization that affect performance, operations and resources. They include all of the elements that exist outside of the organization's boundaries and have the potential to affect a portion or all of the organization, for instance government regulatory agencies, competitors, customers, suppliers and pressure from the public. To manage the organization effectively, managers need to properly understand the environment. It is reasonable to divide environmental factors into two parts, namely, internal and external environments. An organization's internal environment consists of the entities, conditions, events, and factors within the organization that influence choices and activities, especially in employee behaviour. It exposes the strengths and weaknesses found within the organization. Factors that are frequently considered part of the internal environment include the organization's culture, mission statement, and leadership styles. An organization's external environment consists of the entities, conditions, events, and factors surrounding the organization that influence choices and activities and determine its opportunities and threats. It is also called an operating environment. Examples of factors affecting an organization's external environment include customers, public opinion, economic conditions, government regulations, and competition. Thus, taking into account the above analysis, the critical infrastructure operating environment threat can be defined as an unnatural event that may cause the critical infrastructure damage and/or change its operation activity in the way unsafe for it and its operating environment, [1]-[2]. For instance, the critical infrastructure unnatural threats coming from its operating environment are another critical infrastructure activity in its operating environment that can result in an accident with serious consequences for the critical infrastructure and its operating environment, a human error an act of vandalism and a terrorist attack changing the critical infrastructure operation process in an unsafe way.

3.1. Semi-Markov model of critical infrastructure operation process including operating environment threats

We assume that the critical infrastructure operation process modelled in Section 2 can be affected by a number w , $w \in N$, of unnatural threats coming from the critical infrastructure operating environment and mark them by ut_i , $i=1,2,\dots,w$. We define new operation states considering the critical nrastructure operating environment threats as follows:

- the operation states without including operating environment threats

$$z'_i = z_i, i = 1, 2, \dots, v, v \in N; \quad (1)$$

- the operation states including at least 1 and maximum w of operating environment threats

$$z'_i, i = v + 1, v + 2, \dots, v', v' \in N. \quad (2)$$

The maximum value of the number of operation states v' is

$$v \cdot \left[\binom{w}{0} + \binom{w}{1} + \dots + \binom{w}{w} \right] = v \cdot 2^w, \quad (3)$$

This way, we can have:

$$- v \cdot \binom{w}{0} = v \quad (4)$$

operation states without including operating environment threats

$$z'_i = z_i, i = 1, 2, \dots, v; \quad (5)$$

$$- v \cdot \binom{w}{1} = vw \quad (6)$$

operation states including 1 of the operating environment threats ut_i , $i = 1, 2, \dots, w$,

$$z'_i, i = v + 1, v + 2, \dots, v + vw; \quad (7)$$

$$- v \cdot \binom{w}{2} = vw(w-1)/2 \quad (8)$$

operation states including different 2 of the operating environment threats ut_i , $i = 1, 2, \dots, w$,

$$z'_i, i = vw + 1, vw + 2, \dots, vw + vw(w-1)/2; \quad (9)$$

$$- v \cdot \binom{w}{w} = v \quad (10)$$

operation states including all w operating environment threats $ut_i, i=1,2,\dots,w$,

$$z'_i, i = v2^w - v + 1, v2^w - v + 2, \dots, v2^w. \quad (11)$$

Practically more comfortable numeration of the operation states of the critical infrastructure operation process including its operating environment threats is as follows:

- operation states without including operating environment threats by

$$\begin{aligned} z'_i &= z_1 \text{ for } i=1, \quad z'_i = z_2 \text{ for } i=2^w + 1, \dots, \\ z'_i &= z_v \text{ for } i=(v-1)2^w + 1; \end{aligned} \quad (12)$$

- operation states including state z_1 and successively 1, 2 until w operating environment threats $ut_i, i=1,2,\dots,w$, by

$$z'_i, i=2, \dots, 2^w, \quad (13)$$

- operation states including state z_2 and successively 1, 2 until w operating environment threats $ut_i, i=1,2,\dots,w$, by

$$\begin{aligned} z'_i, i &= 2^w + 2, \dots, 2 \cdot 2^w, \\ &\dots; \end{aligned} \quad (14)$$

- operation states including state z_v and successively 1, 2 until w operating environment threats $ut_i, i=1,2,\dots,w$, by

$$z'_i, i=(v-1)2^w + 2, \dots, v \cdot 2^w. \quad (15)$$

In our further considerations, we assume that, the critical infrastructure during its operation process can take $v', v' \in N$, defined above by (12)-(15) different operation states

$$z'_1, z'_2, \dots, z'_v, z'_{v+1}, \dots, z'_{v'}. \quad (16)$$

Further, we define the critical infrastructure new operation process $Z'(t), t \in (-\infty, +\infty)$, related to the critical infrastructure operating environment threats with discrete operation states from the set $\{z'_1, z'_2, \dots, z'_{v'}\}$. Moreover, we assume that the critical infrastructure operation process $Z'(t)$ related to its operating environment threats is a semi-Markov process similar to that one considered in

Section 2 with the conditional sojourn times θ'_{bl} at the operation states z'_b when its next operation state is $z'_l, b, l=1,2,\dots,v', b \neq l$. Under these assumptions, the critical infrastructure operation process may be described by:

- the vector of the initial probabilities $p'_b(0) = P(Z'(0) = z'_b), b=1,2,\dots,v'$, of the critical infrastructure operation process $Z'(t)$ staying at particular operation states at the moment $t=0$

$$[p'_{b'}(0)]_{1 \times v'} = [p'_1(0), p'_2(0), \dots, p'_{v'}(0)]; \quad (17)$$

- the matrix of probabilities $p'_{bl}, b, l=1,2,\dots,v'$, of the critical infrastructure operation process $Z'(t)$ transitions between the operation states z'_b and z'_l

$$[p'_{bl}]_{v' \times v'} = \begin{bmatrix} p'_{11} & p'_{12} & \dots & p'_{1v'} \\ p'_{21} & p'_{22} & \dots & p'_{2v'} \\ \dots & \dots & \dots & \dots \\ p'_{v'1} & p'_{v'2} & \dots & p'_{v'v'} \end{bmatrix}; \quad (18)$$

- the matrix of conditional distribution functions $H'_{bl}(t) = P(\theta'_{bl} < t), b, l=1,2,\dots,v'$, of the critical infrastructure operation process $Z'(t)$ conditional sojourn times θ'_{bl} at the operation states

$$[H'_{bl}(t)]_{v' \times v'} = \begin{bmatrix} H'_{11}(t) & H'_{12}(t) & \dots & H'_{1v'}(t) \\ H'_{21}(t) & H'_{22}(t) & \dots & H'_{2v'}(t) \\ \dots & \dots & \dots & \dots \\ H'_{v'1}(t) & H'_{v'2}(t) & \dots & H'_{v'v'}(t) \end{bmatrix} \quad (19)$$

We assume that the suitable and typical distributions suitable to describe the critical infrastructure operation process $Z'(t)$ conditional sojourn times $\theta'_{bl}, b, l=1,2,\dots,v', b \neq l$, in the particular operation states are of the same kind as that listed in Section 2.2 [22] for the critical infrastructure operation process $Z(t)$ conditional sojourn times θ_{bl} , eventually with different parameters they are dependent on.

3.2. Various cases of critical infrastructure operation process including operating environment threats

In practice, to make the model from Section 3.1 the next step is to identify the unknown parameters of the critical infrastructure operation process $Z'(t)$, i.e. to identify the vector of the initial probabilities $[p'_b(0)]_{1 \times v'}$, the matrix of probabilities of transitions

$[p'_{bl}]_{v \times v'}$, and the matrix of conditional distribution functions $[H'_{bl}(t)]_{v \times v'}$.

The sufficiently accurate evaluation of these parameters can be performed according to the methods and procedures presented in [22] under the conditions that there is the possibility of the statistical data collection coming from empirical realizations of the operation process with the separated operation states including the operating environment threats. In the case these operation process realizations are not available, the less accurate evaluations of the unknown parameters can be performed in the analogous way either applying the procedures included in [22] and using approximate necessary data coming from experts or to ask them for direct approximate evaluation of the unknown parameters of the vector $[p'_b(0)]_{1 \times v'}$, the matrix $[p'_{bl}]_{v \times v'}$ and the matrix of the mean values $[M'_{bl}]_{v \times v'}$ of the critical infrastructure operation process $Z'(t)$ conditional sojourn times θ'_{bl} , $b, l = 1, 2, \dots, v', b \neq l$, at the operation states instead of the matrix of their distributions $[H'_{bl}(t)]_{v \times v'}$.

Another case that can be met in practice is that we have in disposal the statistical evaluations of the parameters including operating environment threats $[p_b(0)]_{1 \times v}$, the matrix $[p_{bl}]_{v \times v}$ and either the matrix of the mean values $[M_{bl}]_{v \times v}$ of the critical infrastructure operation process $Z(t)$ conditional sojourn times θ_{bl} , $b, l = 1, 2, \dots, v', b \neq l$, at the operation states or the the matrix of their distributions $[H_{bl}(t)]_{v \times v}$ without of separation the operation states including the operating environment threats. In this case, to get the evaluations of the unknown parameters of the vector $[p'_b(0)]_{1 \times v'}$, the matrix $[p'_{bl}]_{v \times v'}$ and the matrix of the mean values $[M'_{bl}]_{v \times v'}$ of the conditional sojourn times θ'_{bl} , $b, l = 1, 2, \dots, v', b \neq l$, at the operation states (instead of the matrix of their distributions $[H'_{bl}(t)]_{v \times v'}$) of the critical infrastructure operation process $Z'(t)$ with included and separated operating threats, we proceed as follows.

Since according to Section 3.1, the critical infrastructure operation process can be affected by a number $w, w \in N$, of unnatural threats ut_i , $i = 1, 2, \dots, w$, coming from the critical infrastructure operating environment, we assume that they are random and we mark the probability of the operating environment threat ut_i , $i = 1, 2, \dots, w$, appearance by

$$P_b(ut_i), i = 1, 2, \dots, w, b = 1, 2, \dots, v.$$

Moreover, in this approach, we consider 2 variants:
 variant 1 - the probabilities of the operating

environment threats ut_i , $i = 1, 2, \dots, w$, appearance $P_b(ut_i)$, $i = 1, 2, \dots, w$, $b = 1, 2, \dots, v$, are conditional and concerned with each of the critical infrastructure particular states (they can be different for various operation states);

variant 2 - the probabilities of the operating environment threats ut_i , $i = 1, 2, \dots, w$, appearance $P_b(ut_i)$, $i = 1, 2, \dots, w$, $b = 1, 2, \dots, v$, are unconditional and concerned with the critical infrastructure operation process independently of its particular states.

Further, to get the initial probabilities of the vector $[p'_b(0)]$ of the operation process $Z'(t)$ with separated operation states including the operating environment threats, we distribute the initial probabilities of the vector $[p_b(0)]$ in the following way:

i) variant 1

- if

$$p_b(0) \neq 0, b = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-1)+1}(0) = p_b(0) - [P_b(ut_1) + P_b(ut_2) + \dots + P_b(ut_w)], \quad (20)$$

$$p'_{(w+1)(b-1)+i}(0) = P(ut_i), i = 1, 2, \dots, w, \quad (21)$$

for

$$b = 1, 2, \dots, v;$$

- if

$$p_b(0) = 0, b = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-1)+1}(0) = 0, \quad (22)$$

$$p'_{(w+1)(b-1)+i}(0) = 0, i = 1, 2, \dots, w, \quad (23)$$

for $b = 1, 2, \dots, v$.

ii) variant 2

- if

$$p_b(0) \neq 0, b = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-l)+1}(0) = p_b(0) - p_b(0)[P_b(ut_1) + P_b(ut_2) + \dots + P_b(ut_w)], \quad (24)$$

$$p'_{(w+1)(b-l)+1+i}(0) = p_b(0)P_b(ut_i), \quad i = 1, 2, \dots, w, \quad (25)$$

for $b = 1, 2, \dots, v$;

- if

$$p_b(0) = 0, \quad b = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-l)+1}(0)b(0) = 0, \quad (26)$$

$$p'_{(w+1)(b-l)+1+i}(0) = 0, \quad i = 1, 2, \dots, w, \quad (27)$$

for $b = 1, 2, \dots, v$.

To get the probabilities of transitions between the operation states of the matrix $[p'_{bl}(0)]$ of the operation process $Z'(t)$ with separated operation states including the operating environment threats, we distribute the probabilities of transitions between the operation states of the matrix $[p_{bl}]$ in the following way:

i) variant 1:

- if

$$p_{bl} \neq 0, \quad b, l = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1} = p_{bl} - [P_b(ut_1) + P_b(ut_2) + \dots + P_b(ut_w)], \quad (28)$$

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1+i} = P_b(ut_i), \quad i = 1, 2, \dots, w, \quad (29)$$

for $b, l = 1, 2, \dots, v$;

and we additionally assume that

$$p'_{(w+1)(b-l)+1+i (w+1)(b-l)+1} = 1, \quad i = 1, 2, \dots, w, \quad (30)$$

$$p'_{(w+1)(b-l)+1+i j} = 0, \quad i = 1, 2, \dots, w, \quad j = 1, 2, \dots, v2^w, \quad (31)$$

and $j \neq (w+1)(b-l)+1$;

- if

$$p_{bl} = 0, \quad b, l = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1} = 0, \quad (32)$$

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1+i} = 0, \quad i = 1, 2, \dots, w, \quad (33)$$

for $b, l = 1, 2, \dots, v$.

ii) variant 2:

- if

$$p_{bl}(0) \neq 0, \quad b, l = 1, 2, \dots, v,$$

we replace it by

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1} = p_{bl} - p_{bl}[P_b(ut_1) + P_b(ut_2) + \dots + P_b(ut_w)], \quad (34)$$

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1+i} = p_{bl}P_b(ut_i), \quad i = 1, 2, \dots, w, \quad (35)$$

for $b, l = 1, 2, \dots, v$,

and we additionally assume that

$$p'_{(w+1)(b-l)+1+i (w+1)(b-l)+1} = 1, \quad i = 1, 2, \dots, w, \quad (36)$$

$$p'_{(w+1)(b-l)+1+i j} = 0, \quad i = 1, 2, \dots, w, \quad j = 1, 2, \dots, v2^w, \quad (37)$$

and $j \neq (w+1)(b-l)+1$;

- if

$$p_{bl} = 0, \quad b, l = 1, 2, \dots, v, \quad b \neq l,$$

we replace it by

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1} = 0, \quad (38)$$

$$p'_{(w+1)(b-l)+1 (w+1)(l-l)+1+i} = 0, \quad i = 1, 2, \dots, w, \quad (39)$$

for $b, l = 1, 2, \dots, v$.

The conditions (30)-(31) and (36)-(37) mean that the transitions from the operation states including the operating environment threats is possible only to the corresponding operation states without the operating environment threats.

Finally, as the transformation of the matrix $[H_{bl}(t)]_{v \times v}$ of the critical infrastructure operation process $Z(t)$ conditional sojourn times θ_{bl} , $b, l = 1, 2, \dots, v$, at the operation states without of separation the operation states including the operating environment threats into the matrix $[H'_{bl}(t)]_{v \times v'}$ of the distributions of the conditional

sojourn times θ'_{bl} , $b, l = 1, 2, \dots, v'$, at the operation states of the critical infrastructure operation process $Z'(t)$ with included and separated operating threats on the basis of expert opinions is practically not possible, we transform the corresponding matrix $[M_{bl}]_{v \times v}$ of the mean values of the conditional sojourn times θ_{bl} , $b, l = 1, 2, \dots, v$, at the operation states into the matrix $[M'_{bl}]_{v' \times v'}$ of the mean values of the conditional sojourn times θ'_{bl} , $b, l = 1, 2, \dots, v'$. We proceed, for both variants (variant 1 and variant 2), in the following way:

- if $M_{bl}(0) \neq 0$, $b, l = 1, 2, \dots, v$,

we fix the mean values

$$M^{(w+1)(b-l)+1+i (w+1)(b-l)+1} \quad i = 1, 2, \dots, w, \quad b = 1, 2, \dots, v, \quad (40)$$

on the basis of expert opinions and assume

$$M^{(w+1)(b-l)+1+i j} = 0, \quad i = 1, 2, \dots, w, \quad j = 1, 2, \dots, v^w, \quad (41)$$

and $j \neq (w+1)(b-l)+1$, and

$$M'_{(w+1)(b-l)+1 (w+1)(l-l)+1} = M_{bl} - \sum_{i=1}^w M'_{(w+1)(b-l)+1+i (w+1)(b-l)+1}, \quad (42)$$

for $b, l = 1, 2, \dots, v$;

- if $M_{bl}(0) = 0$, $b, l = 1, 2, \dots, v$,

we replace it by

$$M^{(w+1)(b-l)+1 (w+1)(l-l)+1} = 0, \quad (43)$$

$$M^{(w+1)(b-l)+1 (w+1)(l-l)+1+i} = 0, \quad i = 1, 2, \dots, w, \quad (44)$$

for $b, l = 1, 2, \dots, v$.

4. Conclusion

In the paper there is presented the probabilistic model of the critical infrastructure operation process. Presented model is the basis for further considerations in particular tasks of the EU-CIRCLE project. Next this model will be used to construct the integrated general safety probabilistic model of the critical infrastructure related to its operation process and climate-weather process [3]. The model will be applied to real critical infrastructures such as the port oil piping transportation system and the maritime ferry technical system. The model further

development will be done in the following EU-CIRCLE project reports: [4]-[6], [9]-[12].

Acknowledgments



The paper presents the results developed in the scope of the EU-CIRCLE project titled “A pan – European framework for strengthening Critical Infrastructure resilience to climate change” that has received funding from the European Union’s Horizon 2020 research and innovation programme under grant agreement No 653824. <http://www.eu-circle.eu/>.

References

- [1] EU-CIRCLE Report D1.1. (2015). *EU-CIRCLE Taxonomy*.
- [2] EU-CIRCLE Report D1.4-GMU3. (2016). *Holistic approach to analysis and identification of critical infrastructures within the Baltic Sea area and its surroundings – Formulating the concept of a global network of critical infrastructures in this region (“network of networks” approach)*.
- [3] EU-CIRCLE Report D2.1-GMU3. (2016). *Modelling outside dependences influence on Critical Infrastructure Safety (CIS) – Modelling Climate-Weather Change Process (C-WCP) including Extreme Weather Hazards (EWH)*.
- [4] EU-CIRCLE Report D2.1-GMU4. (2016). *Modelling outside dependences influence on Critical Infrastructure Safety (CIS) - Designing Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) by linking CIOP and C-WCP models*.
- [5] EU-CIRCLE Report D2.2-GMU1. (2016). *Modelling port piping transportation system operation process at the southern Baltic Sea area using the Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) in this region*.
- [6] EU-CIRCLE Report D2.2-GMU2. (2016). *Modelling maritime ferry transportation system operation process at the Baltic Sea area using the Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) in this region*.
- [7] EU-CIRCLE Report D2.2-GMU3. (2016). *Modelling port, shipping and ship traffic and port operation information critical infrastructures network operation process at the Baltic Sea area*

- using the Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) in this region.
- [8] EU-CIRCLE Report D2.2-GMU4. (2016). *Modelling the operation process of the Baltic Sea critical infrastructures global network of interconnected and interdependent critical infrastructures located within the Baltic Sea and ashore around that function collaboratively using the Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWE) in its operating environment ("network of networks" approach).*
- [9] EU-CIRCLE Report D2.3-GMU1. (2016). *Identification methods and procedures of Critical Infrastructure Operation Process (CIOP) including Operating Environment Threats (OET).*
- [10] EU-CIRCLE Report D2.3-GMU3. (2016). *Identification methods and procedures of unknown parameters of Critical Infrastructure Operation Process General Model (CIOPGM) related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH).*
- [11] EU-CIRCLE Report D2.3-GMU4. (2016). *Evaluation of unknown parameters of a port oil piping transportation system operation process related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) at the southern Baltic Sea area.*
- [12] EU-CIRCLE Report D2.3-GMU5. (2016). *Evaluation of unknown parameters of a maritime ferry transportation system operation process related to Operating Environment Threats (OET) and Extreme Weather Hazards (EWH) at the Baltic Sea area.*
- [13] Ferreira, F. & Pacheco, A. (2007). Comparison of level-crossing times for Markov and semi-Markov processes. *Statistics and Probability Letters* 7, 2, 151-157.
- [14] Glynn, P. W. & Haas, P. J. (2006). Laws of large numbers and functional central limit theorems for generalized semi-Markov processes. *Stochastic Models* 22, 2, 201-231.
- [15] Grabski, F. (2002). *Semi-Markov Models of Systems Reliability and Operations Analysis*. System Research Institute, Polish Academy of Science (in Polish).
- [16] Guze, S., Kołowrocki, K. & Soszyńska, J. (2008). Modeling environment and infrastructure influence on reliability and operation processes of port transportation systems. *Journal of Polish Safety and Reliability Association, Summer Safety and Reliability Seminars* 2, 1, 179-188.
- [17] Kołowrocki, K. (2014). *Reliability of Large and Complex Systems*. Amsterdam, Boston, Heidelberg, London, New York, Oxford, Paris, San Diego, San Francisco, Singapore, Sidney, Tokyo, Elsevier.
- [18] Kolowrocki, K. & Soszynska, J. (2009). Modeling environment and infrastructure influence on reliability and operation process of port oil transportation system. *Electronic Journal Reliability & Risk Analysis: Theory & Applications* 2, 3, 131-142.
- [19] Kolowrocki, K. & Soszynska, J. (2009). Safety and risk evaluation of Stena Baltica ferry in variable operation conditions. *Electronic Journal Reliability & Risk Analysis: Theory & Applications* 2, 4, 168-180.
- [20] Kolowrocki, K. & Soszynska, J. (2010). Reliability modeling of a port oil transportation system's operation processes. *International Journal of Performance Engineering* 6, 1, 77-87.
- [21] Kolowrocki, K. & Soszynska, J. (2010). Reliability, availability and safety of complex technical systems: modelling –identification – prediction – optimization. *Journal of Polish Safety and Reliability Association, Summer Safety and Reliability Seminars* 4, 1, 133-158.
- [22] Kołowrocki, K. & Soszyńska-Budny, J. (2011). *Reliability and Safety of Complex Technical Systems and Processes: Modeling - Identification - Prediction – Optimization*. London, Dordrecht, Heidelberg, New York, Springer.
- [23] Limnios, N. & Oprisan, G. (2005). *Semi-Markov Processes and Reliability*. Birkhauser, Boston.
- [24] Mercier, S. (2008). Numerical bounds for semi-Markovian quantities and application to reliability. *Methodology and Computing in Applied Probability* 10, 2, 179-198.
- [25] Soszyńska, J. (2007). *Systems reliability analysis in variable operation conditions*. PhD Thesis, Gdynia Maritime University-System Research Institute Warsaw (in Polish).
- [26] Soszyńska, J., Kołowrocki, K., Blokus-Roszkowska, A. et al. (2010). Prediction of complex technical systems operation processes. *Journal of Polish Safety and Reliability Association, Summer Safety and Reliability Seminars* 4, 2, 379-510.

